

University of Maryland  
Master's in Telecommunications Program  
Sample Placement Exam Questions for ENTS 622

ENTS 622: Introduction to Digital Communications Systems

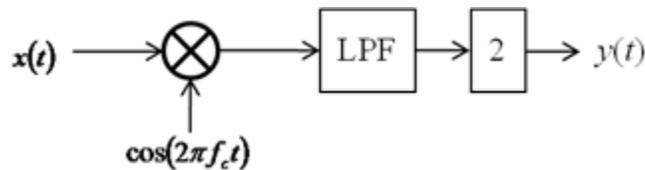
1. Say  $Y(t) = X(t) + A$ , where  $X(t)$  is a random process and  $A$  is a constant, known DC component. Then, please choose the best answer:

- (a)  $Y(t)$ 's autocorrelation function will contain a constant component equal to  $A$ .
- (b)  $Y(t)$ 's autocorrelation function will contain a constant component equal to  $A^2$ .
- (c)  $Y(t)$ 's power spectral density will be shifted by  $A$  in the positive direction with respect to  $X(t)$ 's.
- (d)  $Y(t)$ 's power spectral density will contain a constant component equal to  $A\delta(f+A)$  (where  $\delta(\cdot)$  is the Dirac delta function).

2. Which is the Fourier transform of  $rect(\frac{t}{T}) = \begin{cases} 1, & |t| \leq \frac{T}{2} \\ 0, & \text{otherwise} \end{cases}$

- (a)  $T \text{rect}(fT)$
- (b)  $e^{-j2fT} \text{sinc}^2(f)$
- (c)  $\frac{\text{rect}(f)}{2}(\delta(f - T) + \delta(f + T))$
- (d)  $T \text{sinc}(fT)$

3. In the illustration below,  $x(t)$  is a real narrowband signal, with bandwidth  $2W$  and carrier frequency  $f_c \gg W$ . The low-pass filter (LPF) has bandwidth  $W$  and a gain of 1.



Then  $y(t)$  is

- (a) the complex envelope of  $x(t)$ .
- (b) the quadrature component of  $x(t)$ .
- (c) the in-phase component of  $x(t)$ .
- (d) the envelope of  $x(t)$ .

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4. Concerning DPSK (Differential Phase Shift Keying) and PSK (Phase Shift Keying) modulation, we may say that:

- (a) The symbol error rate for DPSK is less than for PSK, for equal SNR.
- (b) PSK is a constant envelope modulation method.
- (c) DPSK uses non-coherent demodulation.
- (d) Both (b) and (c).

5. The entropy of a discrete memoryless source

- (a) is a lower bound on the average codeword length.
- (b) is equal to the required bandwidth of a communication channel.
- (c) is an upper bound on the SNR of a detector output.
- (d) is zero if and only if none of the symbols' probabilities are equal to 1.

6. If  $X = 48$  in absolute linear scale, then approximately what is  $X$  decreased by 6dB, in absolute linear scale?

- (a) 6
- (b) 12
- (c) 18
- (d) 24

7. If we denote the natural logarithm as  $\ln(\cdot)$ , and the Dirac delta function as  $\delta(\cdot)$ , then please, choose which one is correct:

- (a)  $\int_{-20}^{-1} \frac{3\delta(x+3)}{e^{-x}} dx = \frac{3}{e^3}$
- (b)  $\int_0^{\infty} \delta(t + \frac{1}{2}) e^{-t^2} dt = \frac{\sqrt{\pi}}{2}$
- (c)  $\int_{-2}^{-1} (se^s + 1) \delta(s - \frac{1}{2}) ds = -\frac{1}{e^2}$
- (d)  $\int_1^2 \delta(w + 1) \frac{-3}{w^2} dw = -3 \cdot \ln(2)$

